

Sec 6.4

Linear Inequalities in one Variable

English	Symbols
x is at least 5	$x \geq 5$
x is at most 5	$x \leq 5$
x is between 3 and 5	$3 \leq x \leq 5$
x is less than 5	$x < 5$
x is no more than 5	$x \leq 5$

Rental company charges \$100 per week and \$0.25 per mile to rent a car.

If you can spend no more \$330 on a car rental, how many miles can you drive?

Let x be the number of miles.

$$100 + 0.25x \leq 330$$

$$0.25x \leq 230$$

$$x \leq \frac{230}{0.25}$$

$$x \leq 920$$

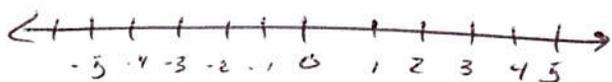
Drive no more than 920 miles.

Sec 6.4

(2)

Solve just like equations, but if you multiply or divide both sides by a negative number, the inequality reverses.

$$-3 \leq 5$$

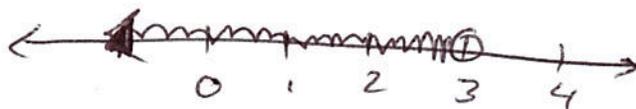


$$-1(-3) \quad -1(5)$$

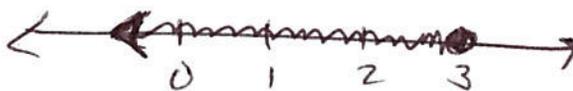
$$3 \geq -5$$

Graph subsets of real numbers

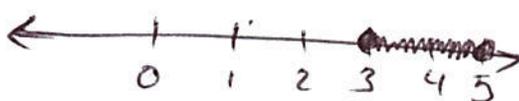
$$\{x : x < 3\}$$



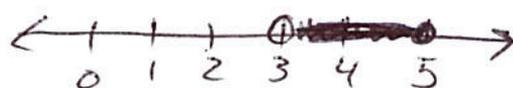
$$\{x : x \leq 3\}$$



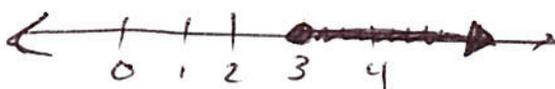
$$\{x : 3 \leq x \leq 5\}$$



$$\{x : 3 < x \leq 5\}$$



$$\{x : x \geq 3\}$$



Example:

(3)

solve the inequality, ~~and~~

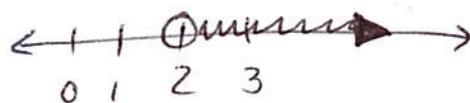
Express the solution in set builder notation and graph it.

$$3x + 5 > 11$$

$$\{x : x > 2\}$$

$$3x > 6$$

$$x > 2$$



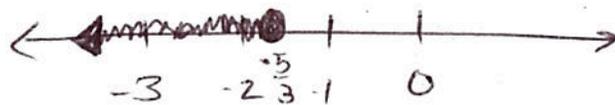
Example: Solve, Express solution in set builder notation, and graph.

$$-3x + 4 \geq 9$$

$$\{x : x \leq -\frac{5}{3}\}$$

$$-3x \geq 5$$

$$x \leq -\frac{5}{3}$$



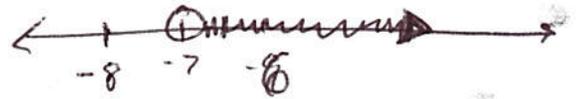
(4)

$$6x - 12 < 8x + 2$$

$$\frac{-6x - 2}{-14} < \frac{-6x - 2}{2x}$$

$$-7 < x$$

$$\{x : x > -7\}$$



Three part : Upper & Lower Bounds

face same way

$$-7 < 2x + 5 \leq 3$$

$$-12 < 2x \leq -2$$

$$-6 < x \leq -1$$

subtract 5

Divide by 2

$$\{x : -6 < x \leq -1\}$$

